

# Classification of Diabetic Retinopathy Using Feature Extraction and Statistical Learning

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Acknowledgement: This research uses the HPC resources at W&M.  
Many thanks to Eric Walter for his kind support.

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& MARY

# Outline

- 1 Medical Background and Technical Details
- 2 Challenges with Feature Extraction
- 3 Image Analysis

## Section 1

# Medical Background and Technical Details

# Diabetic Retinopathy

[Shafqat, 2011]

- Diabetic Retinopathy is a complication that can occur in people suffering from diabetes
- If allowed to progress can cause blindness.
- Can be treated effectively, especially if detected at an early stage before symptoms are present

[American Academy of Ophthalmology]

- Classified in five stages: Not present (0), Mild Non-Proliferative (1), Moderate Non-Proliferative (2), Severe Non-Proliferative (3), Proliferative (4)

# Technical Details

- Data set from Kaggle.

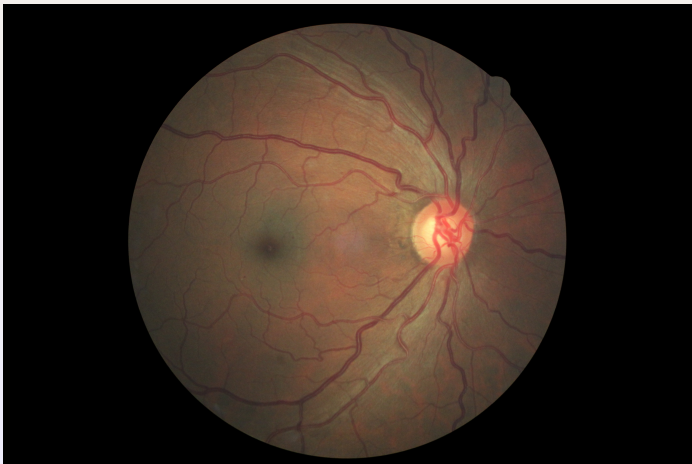
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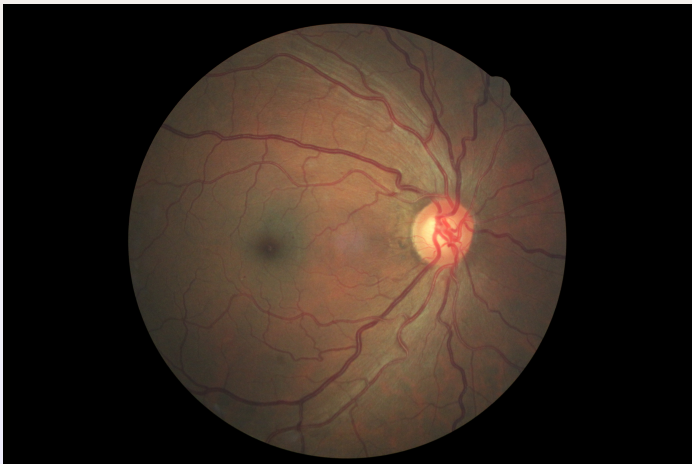
- Data set from Kaggle.
- 35,000 training images with classifications.
- We are using Python, Julia, MATLAB, and R to implement our approach along with GPU computing libraries such as OpenCV and ArrayFire.

## Characteristics of the Retina



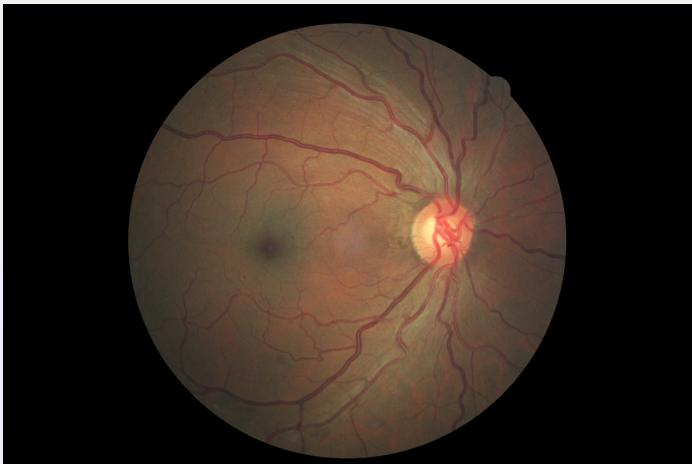


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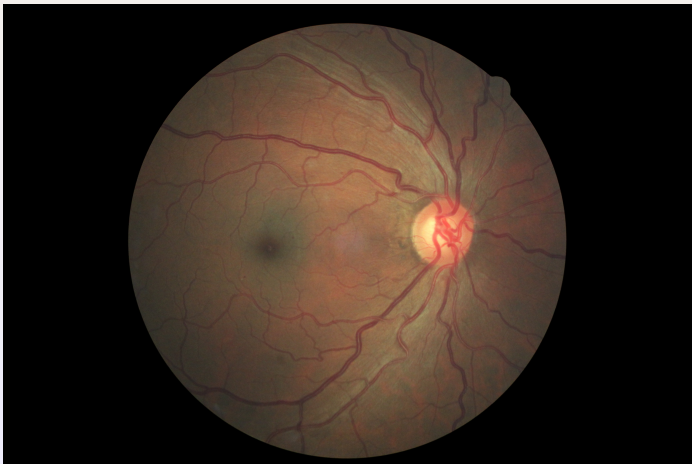
- Optic Nerve

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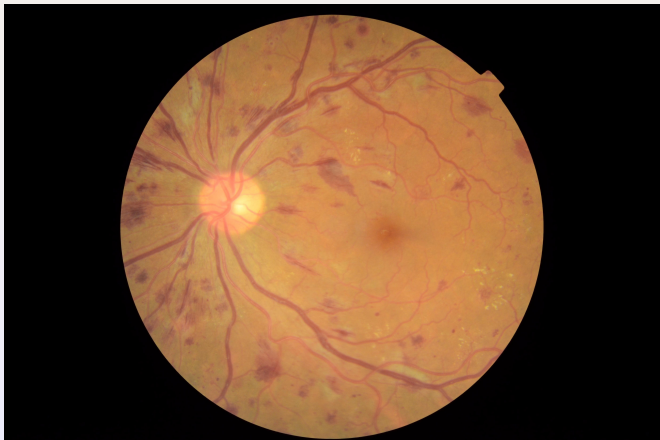
- Optic Nerve
- Blood Vessels

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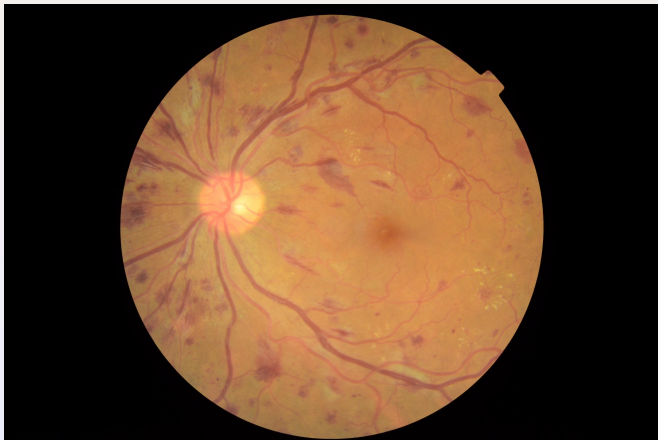
- Optic Nerve
- Blood Vessels
- Macula

# Symptoms



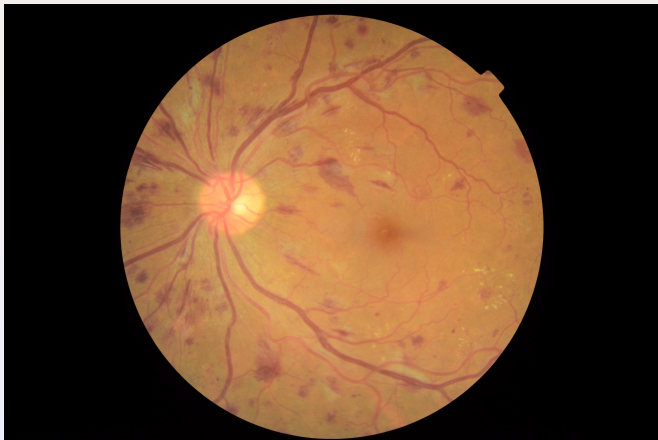
- Microaneurysms ("dots")

# Symptoms



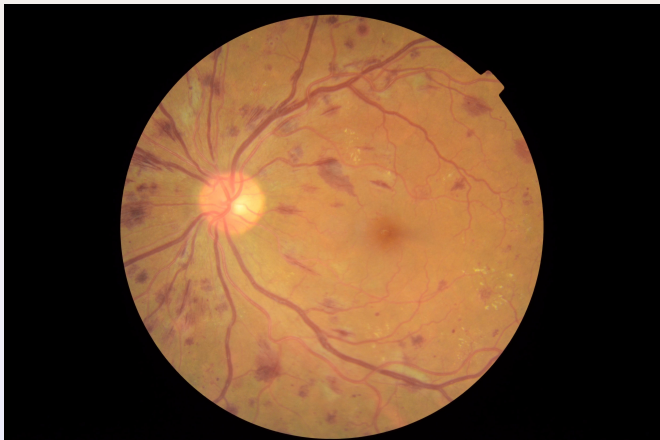
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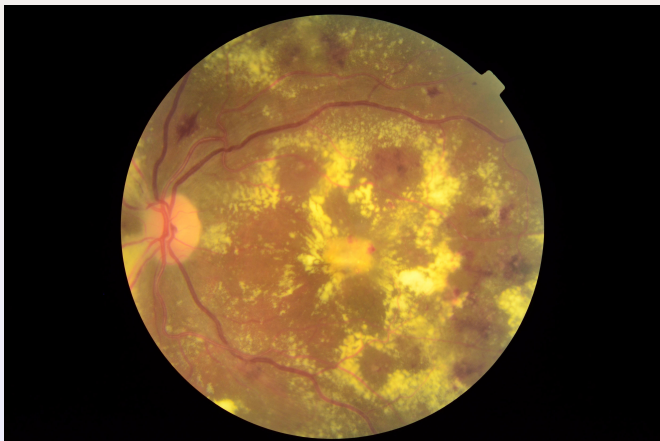
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- Exudates

# Symptoms



- Microaneurysms ("dots")
- Haemorrhages ("blots")
- Exudates
- Tortuosity of Blood Vessels

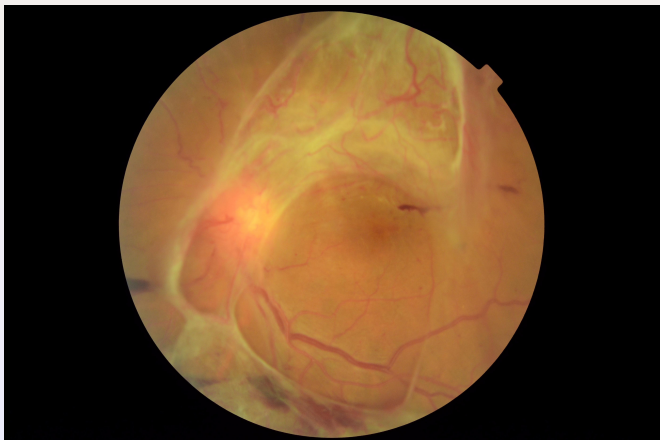
## Proliferative DR



- Cotton Wool Spotting



## Proliferative DR cont.

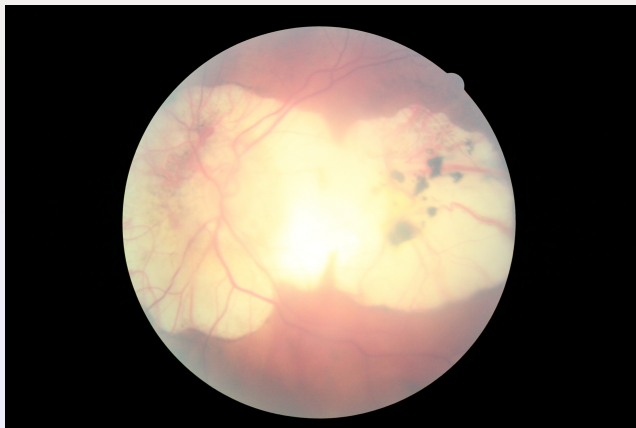


- Neovascularisation

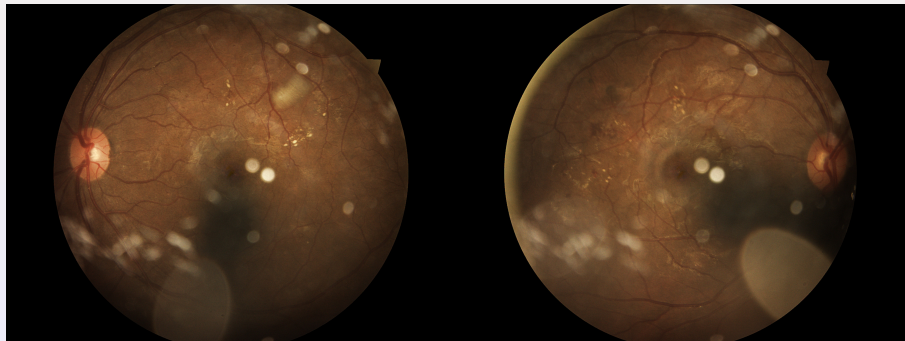
## Section 2

# Challenges with Feature Extraction

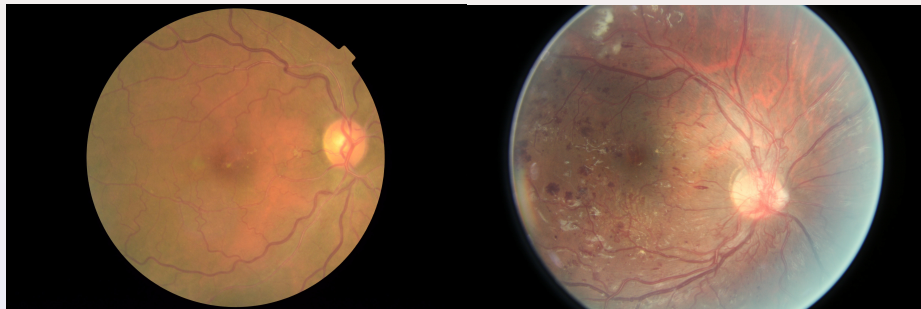
# Misdiagnosed Images



## Deceptive Noise



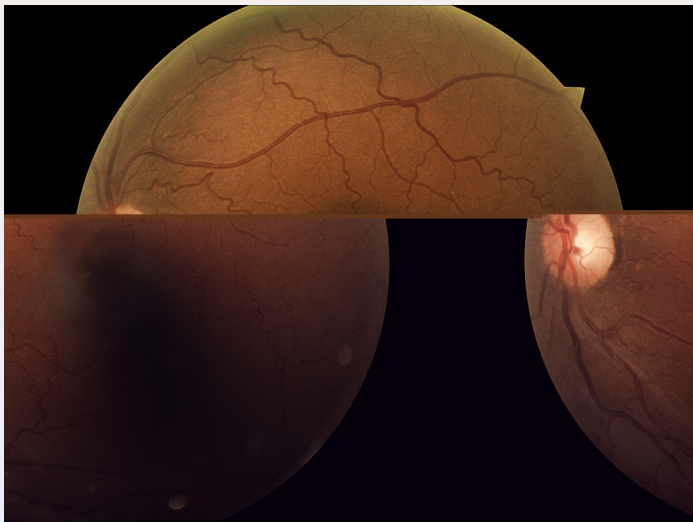
# Images with Different Transformations



- Inversion

- Scale

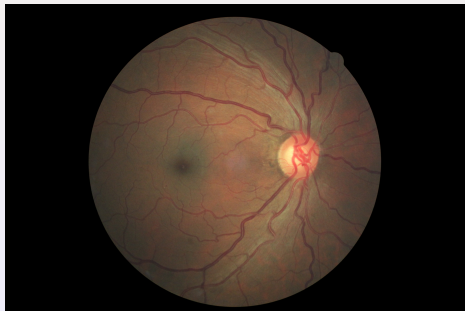
# Bad Images



## Section 3

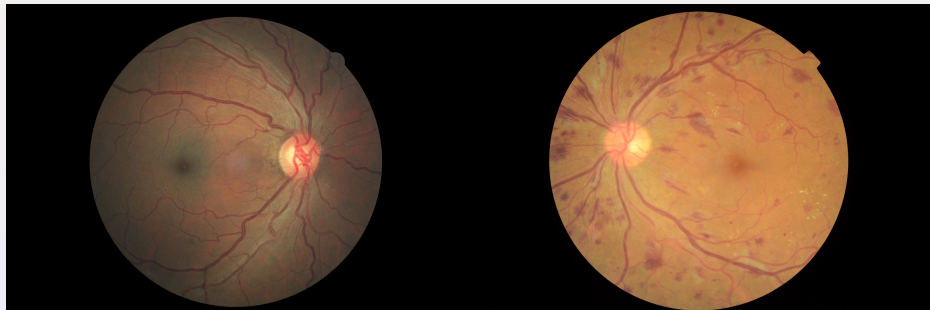
# Image Analysis

## Example Images

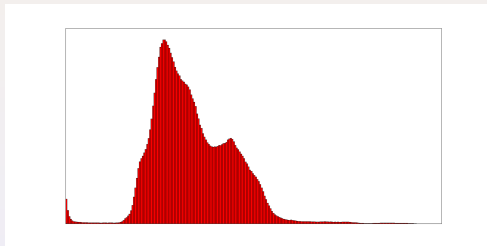




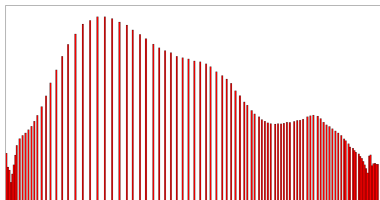
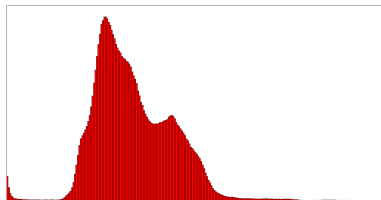
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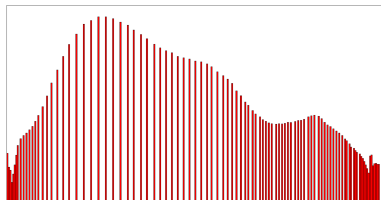
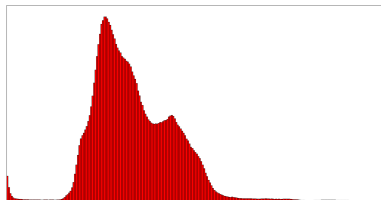
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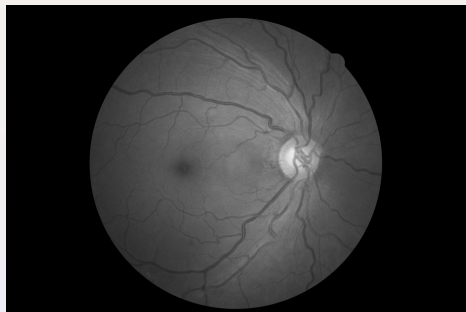
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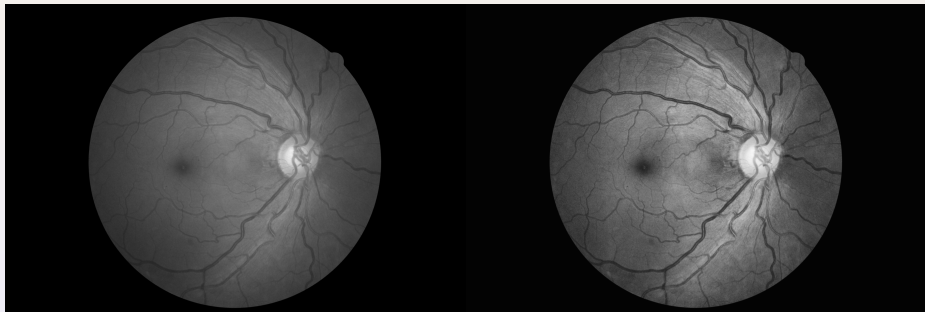
[Gonzalez and Woods, 2008]

- Pixel  $g_{i,j} = \text{floor}((L - 1) \sum_{n=0}^{f_{i,j}} p_n)$
- Where  $L$  is the number of intensity levels in the input image,  $f_{i,j}$  is the original intensity of the pixel, and  $p_n = \frac{\text{number of pixels with intensity } n}{\text{total number of pixels}}$  for  $n = 0, 1, \dots, L - 1$

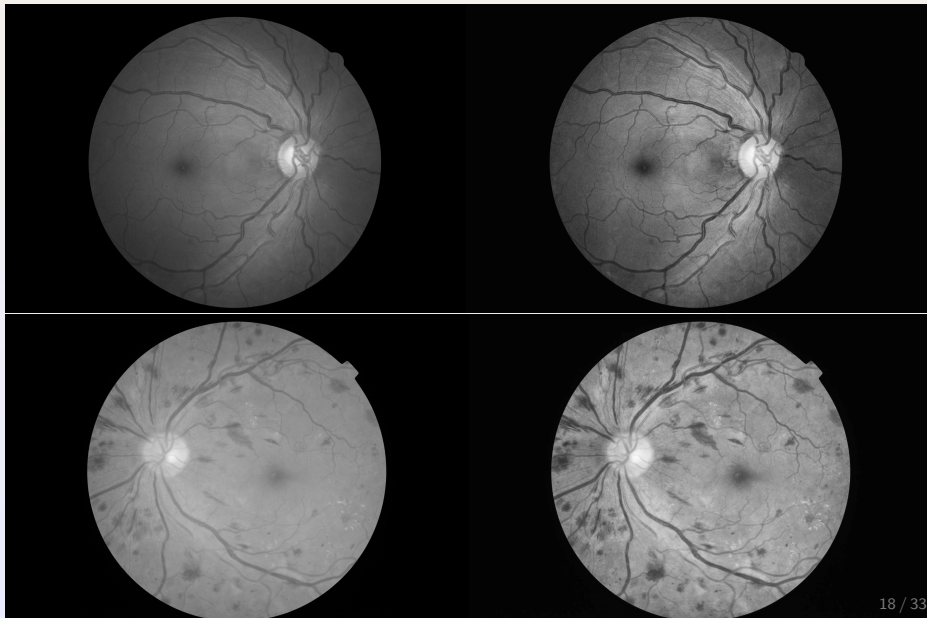
# Results



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# Adaptive Thresholding

[Fisher, Perkins, Walker, and Wolfart, 2003]

- $T = mean$
- $T$  is the threshold value and  $mean$  is the mean value of the pixels of the image



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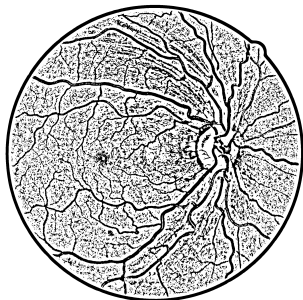
[Fisher, Perkins, Walker, and Wolfart, 2003]

- $T = mean$
- $T$  is the threshold value and  $mean$  is the mean value of the pixels of the image
- This threshold is computed for a neighborhood of specified size

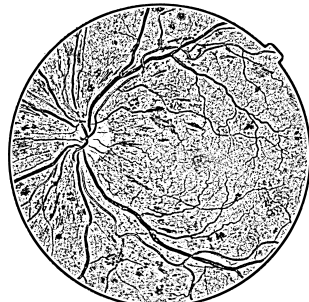
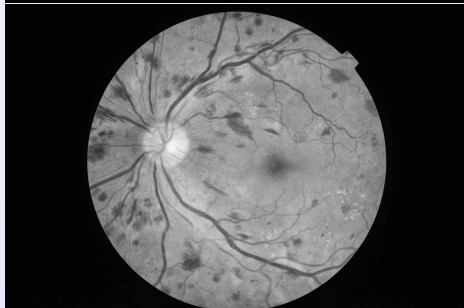
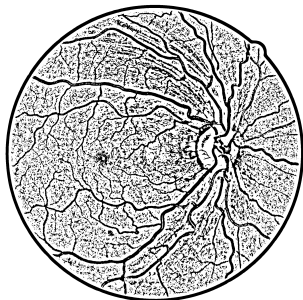
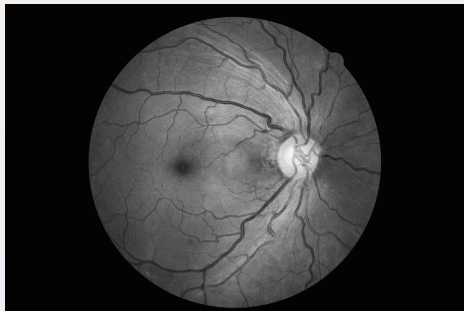
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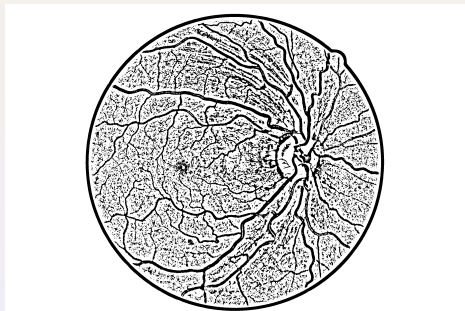
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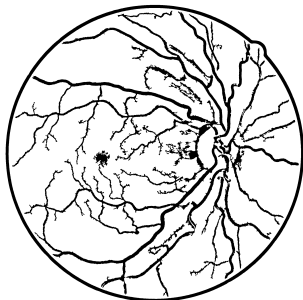
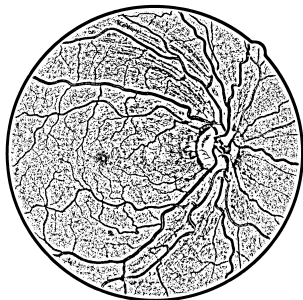
- Eliminate noise by erasing the small connected components

# Results

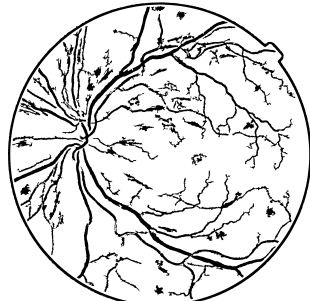
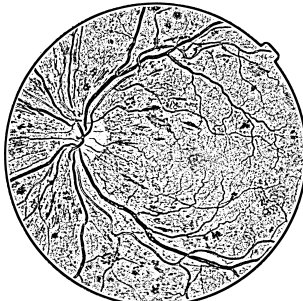
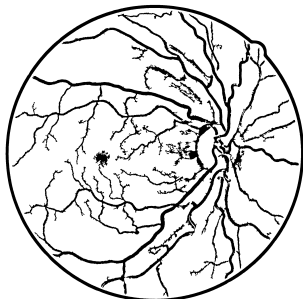
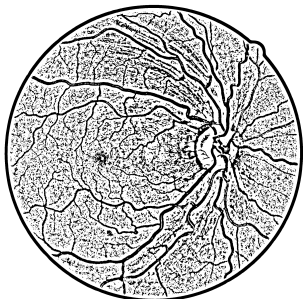




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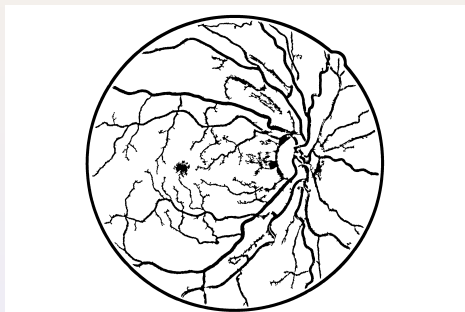
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- Structuring elements:

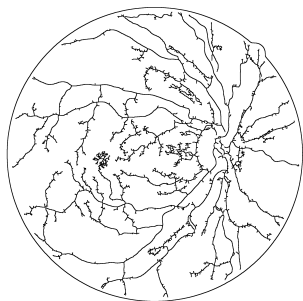
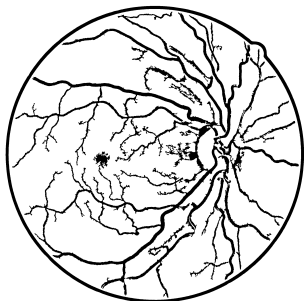
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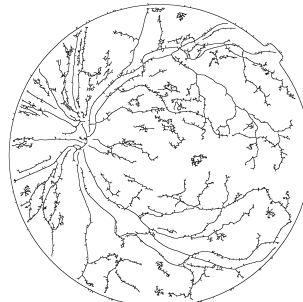
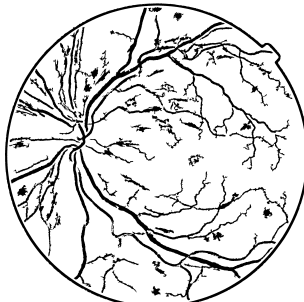
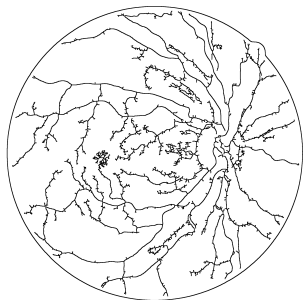
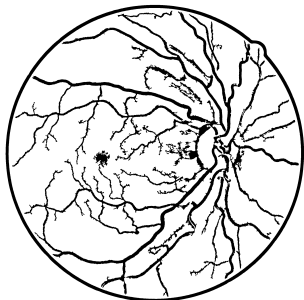
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# Calculating Tortuosity

- Find branchpoints in the skeleton and extract discrete segments

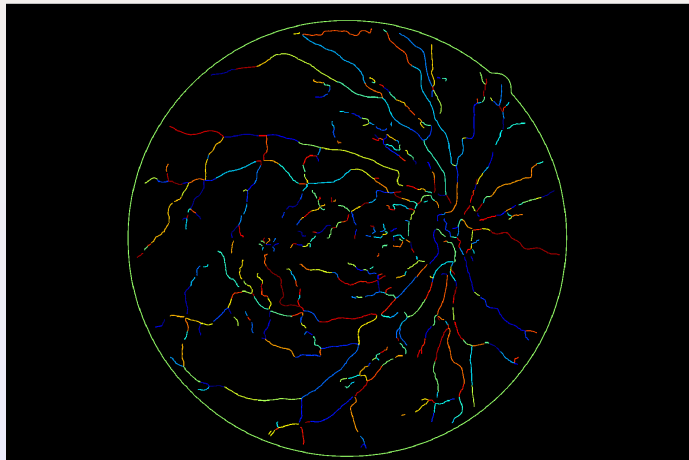
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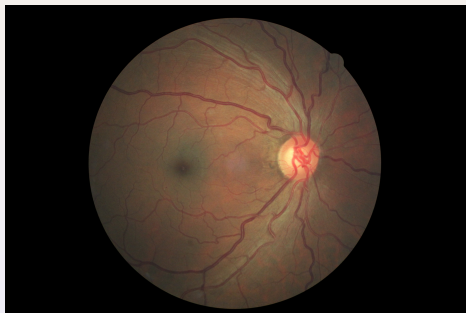
# Calculating Tortuosity

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- $Tortuosity = \frac{L}{C}$
- $L$  is the length of the segment and  $C$  is the Euclidean distance between the endpoints

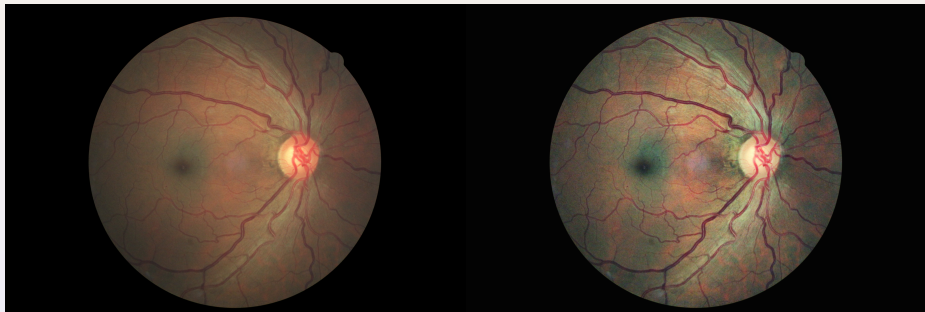
# Example Image



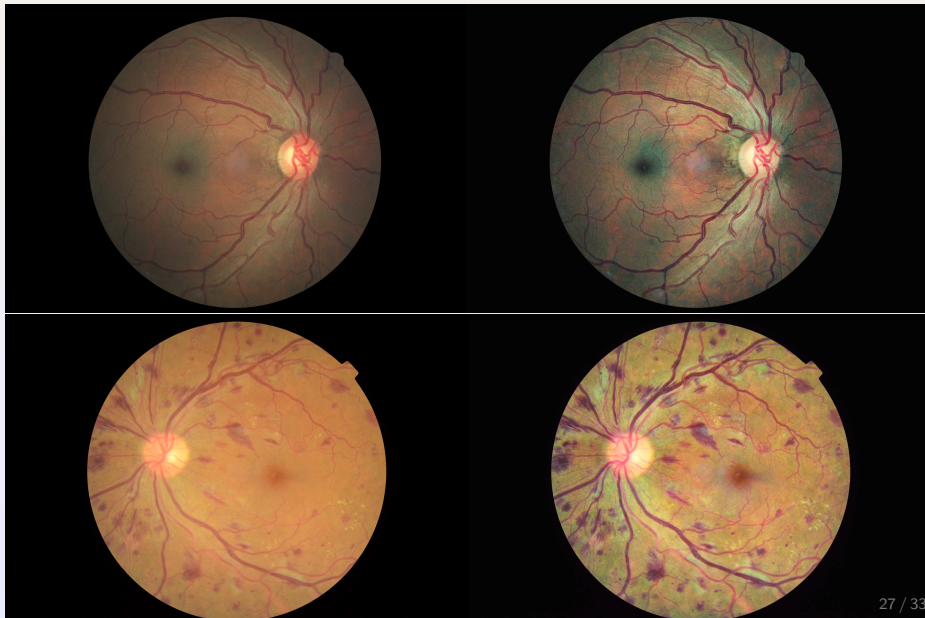
# Separating RGB Channels and Equalizing the Histograms



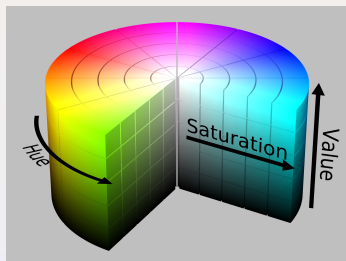
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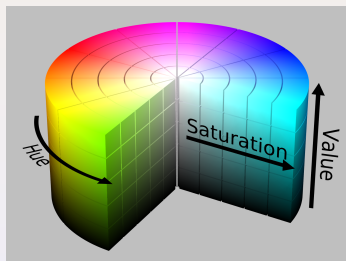
# Detecting Blots and Microaneurysms



- Looked at image on the HSV color model and defined slice of cylinder which would contain blood vessels and microaneurysms

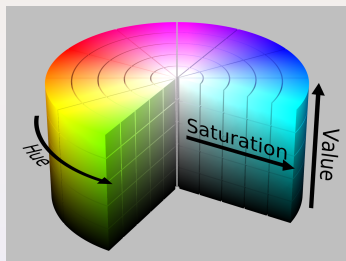


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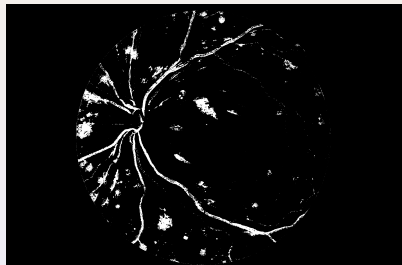
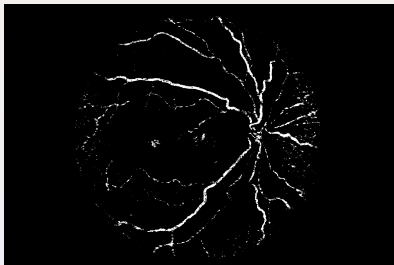
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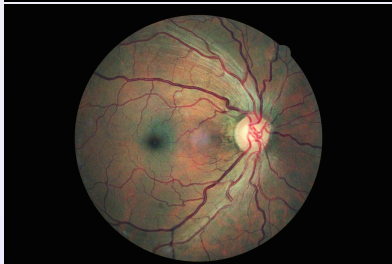
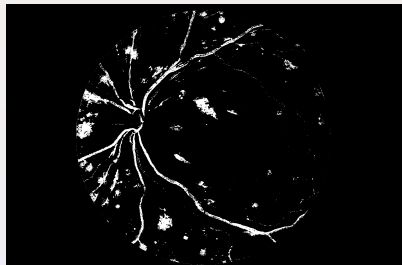
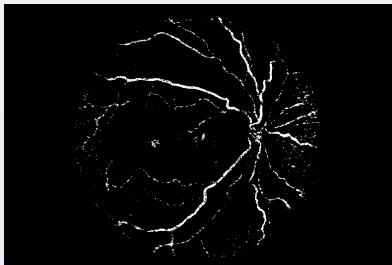


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- Connected components which are in this confidence interval are identified as blood vessels or microaneurysms
- Calculated correlation between  $x$  and  $y$  coordinates of each connected component. Low correlation considered to be a microaneurysm

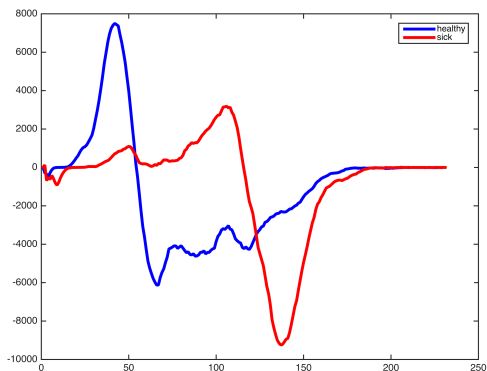
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# Incorporating Computational Homology



- Look at  $b_0$  and  $b_1$  over a range of thresholds
- Calculate Euler Characteristic  $X = b_0 - b_1$  and plot it.
- Count peaks as an additional variable

## Statistical Learning - Logistic Regression

For logistic regression the main idea comes from population biology. If we solve the following differential equation for some initial data we get a CDF:

$$\frac{dN}{dt} = rN \left( 1 - \frac{N}{K} \right). \quad (1)$$

Let's write  $p(x) = Pr(y = 1|x)$  for the response  $y = \begin{cases} 1 & \text{if Class I} \\ 2 & \text{if Class II.} \end{cases}$

If we fit the log-odds to a linear univariate model we have

$$\log \left( \frac{p(x)}{1 - p(x)} \right) = \beta_0 + \beta_1 x. \quad (2)$$

From the log-odds, we can calculate the corresponding probability

$$p(x) = \frac{e^{\beta_0 + \beta_1 x}}{1 + e^{\beta_0 + \beta_1 x}}. \quad (3)$$

## Maximum Likelihood

We use the maximum likelihood concept to estimate the parameters, where the likelihood equation is given by

$$L(\beta_0, \beta_1) = \prod_{i:y_i=1} p(x_i) \prod_{i:y_i=0} (1 - p(x_i)). \quad (4)$$

This likelihood gives the probability of the observed zeros and ones in the data. We choose  $\beta_0$  and  $\beta_1$  to maximize the likelihood of the observed data. Since the logarithmic function is increasing we can maximize instead

$$\frac{1}{n} \sum_{i=1}^n \{I(y_i = 1) \log(p(x_i)) + I(y_i = 2) \log(1 - p(x_i))\} \quad (5)$$

# GLMNET

[Friedman, Hastie, and Tibshirani, 2009]

- When working with a binary classification have response variable  $y = \{1, 2\}$  represent probabilities with predictors

$$Pr(y = 1|x) = \frac{1}{1+e^{-(\beta_0+x^T\beta)}} \text{ and}$$

$$Pr(y = 2|x) = \frac{1}{1+e^{(\beta_0+x^T\beta)}} = 1 - Pr(y = 1|x)$$



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- The idea is to search for  $(\beta_0, \beta) \in \mathbb{R}^{p+1}$  that maximize penalized log likelihood

$$\frac{1}{n} \sum_{i=1}^n \{I(y_i = 1)\log(p(x_i)) + I(y_i = 2)\log(1 - p(x_i))\} - \lambda P_\alpha(\beta) \quad (6)$$

- Where  $P_\alpha(\beta) = \alpha * \|\beta\|_1 + (1 - \alpha) * \|\beta\|_2^2$

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- Where  $P_\alpha(\beta) = \alpha * \|\beta\|_1 + (1 - \alpha) * \|\beta\|_2^2$
- When response variable  $y$  has  $K > 2$  classifications, then for class  $\ell$

$$Pr(y = \ell|x) = \frac{e^{\beta_{0\ell}+x^T\beta_\ell}}{\sum_{k=1}^K e^{\beta_{0k}+x^T\beta_k}}$$